

TOPICAL PAST PAPER QUESTIONS WORKSHEETS

AS & A Level Mathematics (9709) Paper 4

[Mechanics]

Exam Series: February/March 2017 - October/November 2024

Format Type A:

Answers to all questions are provided as an appendix



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Introduction

Each Topical Past Paper Questions Compilation contains a comprehensive collection of hundreds of questions and corresponding answer schemes, presented in worksheet format. The questions are carefully arranged according to their respective chapters and topics, which align with the latest IGCSE or AS/A Level subject content. Here are the key features of these resources:

1. The workbook covers a wide range of topics, which are organized according to the latest syllabus content for Cambridge IGCSE or AS/A Level exams.
2. Each topic includes numerous questions, allowing students to practice and reinforce their understanding of key concepts and skills.
3. The questions are accompanied by detailed answer schemes, which provide clear explanations and guidance for students to improve their performance.
4. The workbook's format is user-friendly, with worksheets that are easy to read and navigate.
5. This workbook is an ideal resource for students who want to familiarize themselves with the types of questions that may appear in their exams and to develop their problem-solving and analytical skills.

Overall, Topical Past Paper Questions Workbooks are a valuable tool for students preparing for IGCSE or AS/A level exams, providing them with the opportunity to practice and refine their knowledge and skills in a structured and comprehensive manner. To provide a clearer description of this book's specifications, here are some key details:

- Title: Cambridge AS & A Level Mathematics (9709) Paper 4 Topical Past Papers
- Subtitle: Exam Practice Worksheets With Answer Scheme
- Examination board: Cambridge Assessment International Education (CAIE)
- Subject code: 9709
- Years covered: February/March 2017 - October/November 2024
- Paper: 4 (Mechanics)
- Number of pages: 849
- Number of questions: 387

Contents

1	Forces and equilibrium	7
2	Kinematics of motion in a straight line	89
3	Momentum	267
4	Newton's laws of motion	279
5	Energy, work and power	413
A	Answers	591

Chapter 1

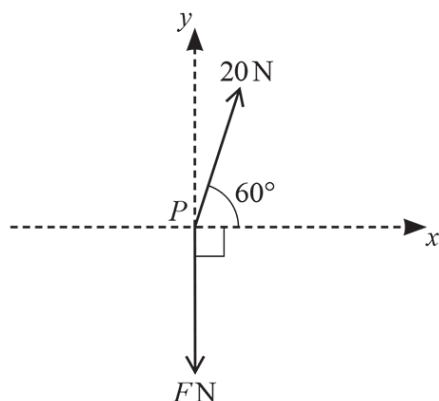
Forces and equilibrium

A diagram showing a particle in equilibrium. Four forces act on it: a 30 N force pointing up and to the left, a $3F$ N force pointing horizontally to the right, a $2F$ N force pointing down and to the right, and an F N force pointing vertically downwards. A dashed horizontal line extends to the left from the particle. The angle between this dashed line and the 30 N force is θ° . A right-angle symbol is shown between the 30 N force and the $2F$ N force. The angle between the $2F$ N force and the vertical F N force is 45° .

Given that the forces are in equilibrium, find the value of F and the value of θ . [6]

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

2. 9709_s24_qp_41 Q: 2



Two forces of magnitudes 20 N and FN act at a point P in the directions shown in the diagram.

- (a) Given that the resultant force has no component in the y -direction, calculate the value of F . [2]

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- (b) Given instead that $F = 10$, find the magnitude and direction of the resultant force. [5]

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Find the values of θ and P . [6]

[illegible]

A diagram showing a particle in equilibrium. Four forces act on the particle, represented by arrows originating from a central point. A horizontal dashed line and a vertical dashed line intersect at the particle. The forces and their directions are: a 12 N force pointing up and to the right at a 30° angle to the vertical; a 24 N force pointing horizontally to the right; an 8 N force pointing down and to the right at a 30° angle to the horizontal; and a 16 N force pointing down and to the left at a 30° angle to the horizontal. A right-angle symbol is shown at the intersection of the dashed lines.

Find the magnitude and direction of the single additional force acting at the same point which will produce equilibrium. [6]

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- (b) Given instead that $F = 10\sqrt{2}$ and $\theta = 45$, find the direction and the exact magnitude the resultant force. [3]

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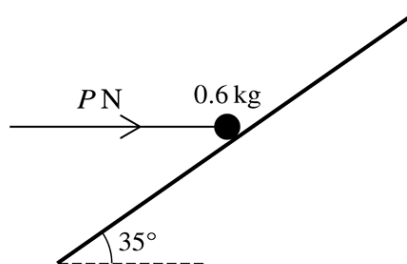
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(b) Verify that $P = 6$ satisfies this equation and find the value of θ . [2]

[illegible]

8. 9709 s23 qp 42 Q: 5



A particle of mass 0.6 kg is placed on a rough plane which is inclined at an angle of 35° to the horizontal. The particle is kept in equilibrium by a horizontal force of magnitude $P\text{ N}$ acting in a vertical plane containing a line of greatest slope (see diagram). The coefficient of friction between the particle and plane is 0.4 .

Find the least possible value of P .

[6]

[illegible]

Find the value of μ for which the system is in limiting equilibrium. [7]

This image shows a full page of white paper with horizontal dashed lines, typical of primary-ruled notebook paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

10. 9709_w23_qp_42 Q: 4

A particle P of mass 0.2 kg lies at rest on a rough horizontal plane. A horizontal force of 1.2 N is applied to P .

- (a) Given that P is in limiting equilibrium, find the coefficient of friction between P and the plane. [3]

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- (b) Given instead that the coefficient of friction between P and the plane is 0.3 , find the distance travelled by P in the third second of its motion. [4]

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Diagram illustrating a pulley system on an inclined plane. A mass of 2.4 kg (labeled A) is on the incline. A mass of 3.3 kg (labeled B) is hanging vertically from a pulley at the top of the incline. The vertical distance from the ground to mass B is 1 m . The angle of the incline is θ° .

(a) It is given that $\theta = 30^\circ$ and the system is in equilibrium with A on the point of moving directly up the plane.

[5]

[illegible]

- (b) It is given instead that $\theta = 20$ and $\mu = 1.01$. The system is released from rest with the string taut.

Find the total distance travelled by A before coming to instantaneous rest. You may assume that A does not reach the pulley and that B remains at rest after it hits the ground. [8]

[illegible]

A diagram showing a particle in equilibrium. Five forces act on the particle: a force of $2F\text{ N}$ acting upwards and to the left at an angle of 40° to the horizontal; a force of GN acting upwards and to the right at an angle of 60° to the horizontal; a force of $F\text{ N}$ acting horizontally to the right; a force of 10 N acting vertically downwards; and a reaction force acting vertically upwards. A right-angle symbol is shown between the horizontal force $F\text{ N}$ and the vertical reaction force.

(a) Given that the forces are in equilibrium, find the values of F and G . [5]

This image shows a full page of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page, typical of notebook or legal stationery. There are no margins, text, or other markings on the page.

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- (b) Given instead that $F = 3$, find the value of G for which the resultant of the forces is perpendicular to the 10 N force. [2]

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A crate of mass 300 kg is at rest on rough horizontal ground. The coefficient of friction between the crate and the ground is 0.5. A force of magnitude X N, acting at an angle α above the horizontal, is applied to the crate, where $\sin \alpha = 0.28$.

This image shows a full page of primary-ruled paper. It consists of multiple horizontal rows, each defined by two parallel dashed lines. The rows are evenly spaced and cover the entire page area, providing a guide for handwriting practice. There are no margins, text, or other markings on the paper.

A diagram showing a particle in equilibrium. Five forces act on the particle, represented by arrows originating from a central point. The forces are:

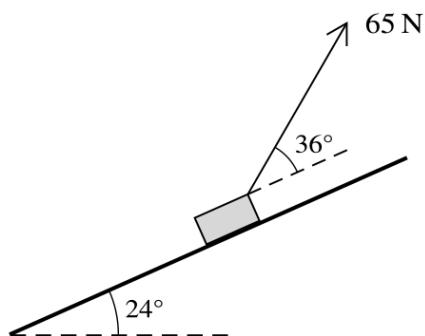
- A vertical force of 60 N acting upwards.
- A horizontal force of 14 N acting to the left.
- A force of 16 N acting downwards and to the left, making an angle of 50° with the horizontal line.
- A force of 20 N acting downwards and to the right, making an angle of 60° with the horizontal line.
- An unlabeled force acting vertically upwards, which is the reaction force from the support.

The horizontal line is dashed to the right of the particle. A right-angle symbol is shown at the central point, indicating that the 14 N force and the vertical reaction force are perpendicular.

[6]

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

16. 9709 _s22 _qp _42 Q: 5



A block of mass 12 kg is placed on a plane which is inclined at an angle of 24° to the horizontal. A light string, making an angle of 36° above a line of greatest slope, is attached to the block. The tension in the string is 65 N (see diagram). The coefficient of friction between the block and plane is μ . The block is in limiting equilibrium and is on the point of sliding up the plane.

Find μ .

[6]

This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting practice. There are no margins, text, or other markings on the page.

Diagram of a right-angled triangle ABC with vertices A and B on a horizontal ceiling. Vertex C is a block of mass 10 kg that is pushed to the right by a force F . The side lengths are $AC = 0.8\text{ m}$ and $BC = 0.6\text{ m}$. The angle at C is 90° .

(a) In the case where $F = 20$, find the tensions in each of the strings. [5]

[illegible]

This image shows a full page of white paper with horizontal dotted lines, typical of primary school handwriting practice paper. The lines are evenly spaced and run across the entire width of the page. There are no margins, text, or other markings present.

Appendix A

Answers

1. 9709_m24_ms_42 Q: 4

Question	Answer	Marks	Guidance
	For resolving in either direction	*M1	Correct number of terms allow sign errors; allow sin/cos mix on θ . Forces that need resolving should be resolved.
	$F + 2F \cos 45 = 30 \sin \theta$	A1	
	$2F \sin 45 + 3F = 30 \cos \theta$	A1	
	$\theta = \tan^{-1} \left(\frac{1 + 2 \cos 45}{2 \sin 45 + 3} \right)$ or $\theta = \sin^{-1} \left(\frac{F + 2F \cos 45}{30} \right)$ or $\theta = \cos^{-1} \left(\frac{2F \sin 45 + 3F}{30} \right)$	DM1	For attempt to find θ . Using their F which can be solved for θ . From equations with correct number of relevant terms, forces that need resolving should be resolved. If $\tan \theta = \frac{\cos \theta}{\sin \theta}$, so have $\theta = \tan^{-1} \left(\frac{2 \sin 45 + 3}{1 + 2 \cos 45} \right)$, then allow M1.
	$\left[F^2 (3 + 2 \sin 45)^2 + F^2 (1 + 2 \cos 45)^2 = 30^2 \Rightarrow \right]$ $F = \frac{30^2}{\sqrt{(3 + 2 \sin 45)^2 + (1 + 2 \cos 45)^2}}$ or $F = \frac{30 \sin \theta}{1 + 2 \cos 45}$ or $F = \frac{30 \cos \theta}{3 + 2 \sin 45}$	DM1	For attempt to find F . From equations with the correct number of relevant terms, forces that need resolving should be resolved. Using their θ .
	$F = 5.96$ [5.96270...] and $\theta = 28.7$ [28.6750...]	A1	Awrt to 5.96 and 28.7. Allow 5.97.
		6	

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2. 9709_s24_ms_41 Q: 2

Question	Answer	Marks	Guidance
(a)	$F = 20 \sin 60$	M1	Attempt to resolve in y-direction; 2 terms; must be $20 \cos 60$ or $20 \sin 60$ and must be linked to F (can be implied by the correct answer seen only).
	$= 17.3 \text{ N}$	A1	AWRT 17.3 (17.320508...) or $10\sqrt{3}$.
		2	

Question	Answer	Marks	Guidance
(b)	For resolving in any direction	*M1	Correct number of terms; allow sin/cos mix; allow sign errors.
	(Horizontal component = $X = R \cos \theta = \pm(20 \cos 60)$ [± 10] (Vertical component = $Y = R \sin \theta = \pm(20 \sin 60 - 10)$ [$= \pm 7.3205 \dots$]	A1	For both correct.
	Magnitude = $\sqrt{(20 \sin 60 - 10)^2 + (20 \cos 60)^2}$ [$= 12.393136 \dots$]	DM1	OE – correct number of terms.
	Angle = $\tan^{-1} \left(\frac{20 \sin 60 - 10}{20 \cos 60} \right)$ [$= 36.206023 \dots$]	DM1	OE (e.g. reciprocal) - correct number of terms.
	Magnitude = 12.4 N and Direction = 36.2° above (positive) x-axis	A1	OE for direction e.g. 36.2° anticlockwise from (positive) x-direction, 36.2° above the horizontal. Possibly seen on a diagram. (Radians: 0.63191... to 3sf or better)
		5	

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3. 9709_s24_ms_42 Q: 3

Question	Answer	Marks	Guidance
	Resolving either direction to get an equation	*M1	Correct number of relevant terms; allow sign errors; allow sin/cos mix.
	$10 \cos 25 = 2 \cos 40 + 16 \sin \theta$ $\left[\begin{array}{l} 9.06307787 = 1.532088886 + 16 \sin \theta \\ 7.530988984 = 16 \sin \theta \\ \sin \theta = 0.4706868115 \end{array} \right]$	A1	
	$P = 10 \sin 25 + 16 \cos \theta + 2 \sin 40$ $\left[\begin{array}{l} P = 4.226182617 + 16 \cos \theta + 1.285575219 \\ P = 5.511757837 + 16 \cos \theta \end{array} \right]$	A1	This may be with <i>their</i> θ .
	Attempt to solve for $\theta = \sin^{-1} \left(\frac{10 \cos 25 - 2 \cos 40}{16} \right)$	DM1	From equation(s) with correct number of relevant terms. Must be a numerical expression for θ .
	Attempt to solve for $P = 10 \sin 25 + 16 \cos(\text{their } \theta) + 2 \sin 40$	DM1	From equation(s) with correct number of relevant terms. Using <i>their</i> θ . Must be a numerical expression for P .
	$\theta = 28.1$ AND $P = 19.6$	A1	28.07888819 and 19.6285636. AWRT 28.1 and AWRT 19.6 from correct work.
		6	

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4. 9709_w24_ms_41 Q: 6

Question	Answer	Marks	Guidance
	Attempt at resolving perpendicular to the plane to get an equation	*M1	Correct number of relevant terms, allow sign errors, allow sin/cos mix, allow g missing. For reference $R = 1.2g \times \cos 16.26... + P \times \sin 16.26...$ - allow with an angle of 16 or better.
	$R = 1.2g \times \frac{24}{25} + P \times \frac{7}{25}$	A1	$R = 11.52 + 0.28P$ or $R = \frac{288}{25} + \frac{7}{25}P$.
	Attempt at resolving parallel to the plane to get an equation	*M1	Correct number of relevant terms, allow sign errors, allow sin/cos mix, allow g missing. For reference $F + P \times \cos 16.26... = 1.2g \times \sin 16.26...$ allow with an angle of 16 or better.
	$F + P \times \frac{24}{25} = 1.2g \times \frac{7}{25}$	A1	$F + 0.96P = 3.36$ or $F + \frac{24}{25}P = \frac{84}{25}$.
	Use of $F = 0.15R$ to get an equation in P only	DM1	Dependent on both previous M marks – where R is initially a linear combination of a P component and a weight component (or a mass component). $1.2g \times \frac{7}{25} - P \times \frac{24}{25} = 0.15 \times \left(1.2g \times \frac{24}{25} + P \times \frac{7}{25} \right)$.
	Solve to get $P = 1.63$	A1	Allow $\frac{272}{167}, 1.62874...$
		6	

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5. 9709_w24_ms_43 Q: 2

Question	Answer	Marks	Guidance
	Resolving either direction	M1	With correct number of relevant terms. Allow sin/cos mix. Allow sign errors. Do not allow 'forces to the left = forces to the right' e.g. $12\cos 30 - 8\sin 30 = 16\sin 30$ unless subsequently 'corrected'.
	$\pm(12\sin 30 + 24 + 8\cos 30 - 16\cos 30) [= F_x \text{ or } F \cos \theta \text{ or } F \sin \alpha]$	A1	$F_x = \pm(30 - 4\sqrt{3})$ $[= 23.07...]$.
	$\pm(12\cos 30 - 8\sin 30 - 16\sin 30) [= F_y \text{ or } F \sin \theta \text{ or } F \cos \alpha]$	A1	$F_y = \pm(6\sqrt{3} - 12)$ $[= -1.607...]$.
	$F = \sqrt{(6\sqrt{3} - 12)^2 + (30 - 4\sqrt{3})^2}$ $F = \frac{30 - 4\sqrt{3}}{\cos(\text{their } \theta)}$ $F = \frac{6\sqrt{3} - 12}{\sin(\text{their } \theta)}$	M1	Attempt to find F . Must have correct number of relevant terms. (Forces must have or not have components as required). All forces resolved/not resolved as appropriate, but allow consistent sin/cos muddle. Allow use of their θ provided correctly derived from equations with the correct number of relevant terms.
	$\theta = \tan^{-1} \left(\frac{6\sqrt{3} - 12}{30 - 4\sqrt{3}} \right)$ $\theta = \cos^{-1} \left(\frac{30 - 4\sqrt{3}}{\text{their } F} \right)$ Note: this will not give the correct answer unless F given to several significant figures $\theta = \sin^{-1} \left(\frac{6\sqrt{3} - 12}{\text{their } F} \right)$	M1	Attempt to find θ . Must have correct number of relevant terms. (Forces must have or not have components as required). All forces resolved/not resolved as appropriate, but allow consistent sin/cos muddle. Allow upside down so $\tan^{-1} \left(\frac{30 - 4\sqrt{3}}{6\sqrt{3} - 12} \right)$. Allow use of their F provided correctly derived from equations with the correct number of relevant terms. Note: watch for use of $\sin^{-1} \left(\frac{6\sqrt{3} - 12}{30 - 4\sqrt{3}} \right)$ or $\sin^{-1} \left(\frac{1.607}{23.07} \right)$ which leads to correct answer of angle 4.0° scores M0A0.

Question	Answer	Marks	Guidance
	$F = 23.1 \text{ N}$ $\theta = 3.99^\circ$ above the negative x -axis oe	A1	[23.1277...] Both correct Allow 4.0° but not simply 4° . [3.986...] Allow answers about the direction such as 'Above the west', 'north of west' etc, or clockwise 183.99 from x axis, or resultant sketch with angle indicated. If not specified in working please check original diagram to see if direction specified there instead. Allow a bearing of 274.0° . Allow explanation of direction that could be drawn uniquely. Or e.g. 86.0° to left of the y -axis or 176.0° from the positive x -axis.
		6	

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6. 9709_s23_ms_41 Q: 5

Question	Answer	Marks	Guidance
(a)	Resolving either direction.	M1	3 terms; allow sign errors and allow sin/cos mix. Must be an equation with either $= 0$ or with an attempt to balance forces.
	Vertical: $F \sin \theta + 40 \sin 60 - 50 = 0$	A1	$[F \sin \theta = 50 - 20\sqrt{3} = 15.358...]$
	Horizontal: $F \cos \theta + 10 - 40 \cos 60 = 0$	A1	$[F \cos \theta = 10]$
	$\theta = \tan^{-1}(5 - 2\sqrt{3})$	M1	Attempt to solve for θ ; one missing term in total $\theta = \tan^{-1} 1.535898...$
	$F = \sqrt{15.358...^2 + 10^2}$	M1	Attempt to solve for F : one missing term in total.
	$\theta = 56.9, F = 18.3$	A1	Both correct (18.327530..., 56.932462...).
		6	
(b)	$(Y =) \pm (10\sqrt{2} \sin 45 + 40 \sin 60 - 50) [= \pm(20\sqrt{3} - 40)]$	B1	Allow non-exact values for $\sqrt{2}$ etc. in correct expression.
	$(X =) \pm (10\sqrt{2} \cos 45 + 10 - 40 \cos 60) [= 0]$	B1	Allow non-exact values for $\sqrt{2}$ etc. in correct expression. Could be implied by correct answer.
	Resultant force is $40 - 20\sqrt{3}$ (N) in the same direction as the 50(N) force.	B1	Allow vertically downwards, south, 180° , negative y -direction. Resultant force must be exact and positive (so $20\sqrt{3} - 40$ is B0).
		3	

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7. 9709_s23_ms_42 Q: 3

Question	Answer	Marks	Guidance
(a)	Resolving either direction.	M1	Correct number of terms, allow sign errors, allow sin/cos mix. Do not allow with just $\sin \alpha$ and $\cos \alpha$.
	$(33+15) \times \frac{3}{5} = P \cos \theta + 30 \cos \theta$ OR $(33+15) \cos \left(\tan^{-1} \frac{4}{3} \right) = P \cos \theta + 30 \cos \theta$ OR $19.8 + 9 = P \cos \theta + 30 \cos \theta$	A1	OE, but see note for final A1. Allow: $28.8 = (P+30) \cos \theta$ $(33+15) \cos 53(.1) = P \cos \theta + 30 \cos \theta$ $19.81 + 9.01 = P \cos \theta + 30 \cos \theta$ $19.86 + 9.03 = P \cos \theta + 30 \cos \theta$.
	$15 \times \frac{4}{5} + 30 \sin \theta = 33 \times \frac{4}{5} + P \sin \theta$ OR $15 \sin \left(\tan^{-1} \frac{4}{3} \right) + 30 \sin \theta = 33 \sin \left(\tan^{-1} \frac{4}{3} \right) + P \sin \theta$ OR $12 + 30 \sin \theta = 26.4 + P \sin \theta$	A1	OE, but see note for final A1. Allow: $14.4 = (30-P) \sin \theta$ $15 \sin 53(.1) + 30 \sin \theta = 33 \sin 53(.1) + P \sin \theta$ $12.00 + 30 \sin \theta = 26.39 + P \sin \theta$ $11.98 + 30 \sin \theta = 26.35 + P \sin \theta$.
	[Use $\cos^2 \theta + \sin^2 \theta = 1$ with] $\cos \theta = \frac{28.8}{P+30}$ and $\sin \theta = \frac{14.4}{30-P}$ to get $\left(\frac{14.4}{30-P} \right)^2 + \left(\frac{28.8}{P+30} \right)^2 = 1$	A1	AG. Must have evidence of where 28.8 and 14.4 come from. A0 for any error seen. A0 if use of inexact angles seen. Any inexact decimals seen for force components, i.e. if 14.4 and/or 28.8 have come from rounding to 3sf, scores M1A1A1A0 max 3/4. If exact values of $\sin \alpha$ and $\cos \alpha$ not shown (e.g. $28.8 = (P+30) \cos \theta$ or $14.4 = (30-P) \sin \theta$ from no working), this scores M1A1A1A0 max 3/4 marks.
		4	

Question	Answer	Marks	Guidance
(b)	Sub $P=6$ into $\left(\frac{14.4}{30-P} \right)^2 + \left(\frac{28.8}{P+30} \right)^2$ to get $\left[\left(\frac{14.4}{24} \right)^2 + \left(\frac{28.8}{36} \right)^2 \right] = \left(\frac{3}{5} \right)^2 + \left(\frac{4}{5} \right)^2 = 0.36 + 0.64 = 1$	B1	Must see either $\left(\frac{3}{5} \right)^2 + \left(\frac{4}{5} \right)^2 = 1$ or $0.36 + 0.64 = 1$ as minimum working.
	$\theta = 36.9$	B1	AWRT 36.9 .
		2	

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8. 9709_s23_ms_42 Q: 5

Question	Answer	Marks	Guidance
	Attempt at resolving parallel or perpendicular to the plane.	*M1	3 terms, allow sign errors, allow sin/cos mix, allow g missing. Forces that need resolving should be resolved, forces that do not need resolving should not be resolved.
	$R = P \sin 35 + 0.6g \cos 35$ [$R = (0.573\dots)P + 4.914\dots$]	A1	
	$F + P \cos 35 = 0.6g \sin 35$ [$F + (0.819\dots)P = 3.441\dots$]	A1	Their F .
	Use of $F = 0.4R$	*M1	Where R is initially a linear combination of a P component and a weight component (or a mass component).
	Solve for P .	DM1	From equations with the correct number of relevant resolved terms. $R = \frac{0.6g}{\cos 35 + 0.4 \sin 35} = 5.7222$. Must get to $P = \dots$, e.g. $P = \frac{0.6g \sin 35 - 0.4 \times 0.6g \cos 35}{\cos 35 + 0.4 \sin 35}$. If no working seen, allow this mark if correct solution for their equations. If $F \leq 0.4R$ used, it should be used correctly. e.g. $0.6g \sin 35 - P \cos 35 \leq 0.4(P \sin 35 + 0.6g \cos 35)$.
	$P = 1.41$	A1	AWRT 1.41 . If $P \geq 1.41$ seen, must then state the least value explicitly for A1.

Question	Answer	Marks	Guidance
	Alternative for Question 5: Resolving vertically and horizontally		
	Attempt at resolving vertically or horizontally.	*M1	3 terms, allow sign errors, allow sin/cos mix, allow g missing. Forces that need resolving should be resolved, forces that do not need resolving should not be resolved.
	$R \cos 35 + F \sin 35 = 0.6g$	A1	Their F or R .
	$P + F \cos 35 = R \sin 35$	A1	Their F or R .
	Use of $F = 0.4R$	*M1	To get 2 equations, one in R (or F) and the other in P and R (or P and F) from resolved equations with correct number of relevant terms. Allow g missing.
	Solve for P	DM1	From equations with the correct number of relevant resolved terms. May see $R = \frac{0.6g}{\cos 35 + 0.4 \sin 35} = 5.7222$; Must get to $P = \dots$, e.g. $P = \frac{0.6g \sin 35 - 0.4 \times 0.6g \cos 35}{\cos 35 + 0.4 \sin 35}$. If no working seen, allow this mark if correct solution for their equations.
	$P = 1.41$	A1	AWRT 1.41 .
		6	

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9. 9709_w23_ms_41 Q: 5

Question	Answer	Marks	Guidance
	Resolving parallel to the slope at A or B to form an equation.	*M1	Correct number of terms; allow sign errors; allow sin/cos mix.
	$1.6g \sin 50 - T - F_B = 0$	A1	If using the same F_s , then M1A1A0B1 max.
	$T - F_A - 1.2g \sin 40 = 0$	A1	System equation (must be four different terms): $1.6g \sin 50 - F_B - F_A - 1.2g \sin 40 = 0$ only scores M1A1A1. Any sign errors scores M1 only.
	$R_A = 1.2g \cos 40$ or $R_B = 1.6g \cos 50$	*B1	Either correct. Must be explicitly linked to the correct contact (so could be seen on a diagram), or as part of a resolving parallel to the slope equation(s) (so must be combined with μ).
	$F_A = 1.2g \mu \cos 40$ or $F_B = 1.6g \mu \cos 50$	*M1	Use of $F = \mu R$ at either A or B . Must be explicitly linked to the correct contact (could be seen on a diagram) or as part of a resolving parallel to the slope equation(s). Allow sin/cos mix error only.
	$1.6g \sin 50 - 1.6g \mu \cos 50 = 1.2g \sin 40 + 1.2g \mu \cos 40$	DM1	Eliminating T , F_A and F_B to form an equation in μ only.
	$\left[\mu = \frac{1.6g \sin 50 - 1.2g \sin 40}{1.2g \cos 40 + 1.6g \cos 50} \right] \Rightarrow \mu = 0.233$	A1	0.23326119...
		7	

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10. 9709_w23_ms_42 Q: 4

Question	Answer	Marks	Guidance
(a)	$R = 0.2g$	B1	
	$1.2 = \mu \times 0.2g$	M1	Resolve horizontally and using $F = \mu R$ to get an equation in μ ; 2 relevant terms.
	$\mu = 0.6$	A1	oe
		3	
(b)	$1.2 - 0.3 \times 0.2g = 0.2a$	*M1	Resolve horizontally using Newton's Second Law; 3 relevant terms; allow sign errors; $R = 0.2g$ only.
	$a = 3$	A1	$0.6 = 0.2a$ only seen, allow with BOD, but if 0.6 as friction being used as resultant force, this is M0A0.
	$s_3 = 0 + \frac{1}{2} \times 3 \times 3^2 [= 13.5] s_2 = 0 + \frac{1}{2} \times 3 \times 2^2 [= 6]$	DM1	For use of $s = ut + \frac{1}{2}at^2$ (or a complete method) to find a distance at least once with $u = 0$ and their positive a and $t = 2$ or $t = 3$.
	Distance = $13.5 - 6 = 7.5$ m	A1	www
		4	

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11. 9709_w23_ms_43 Q: 7

Question	Answer	Marks	Guidance
(a)	Resolving for both particles or for the system to form equation(s)	M1*	Must have correct number of terms. Allow sign errors. Allow sin/cos mix. Allow g missing. M0 if acceleration included unless subsequently equated to zero. Masses must be appropriate for their equation(s). Forces must have components (or not) as required.
	Either $T - F - 2.4g \sin 30 = 0$ AND $3.3g - T = 0$ Or $3.3g - F - 2.4g \sin 30 = 0$	A1	Both correct or system correct. May get $F = 21$. Can be with a wrong non-zero F .
	$R = 2.4g \cos 30 \quad [= 12\sqrt{3} = 20.7846...]$	B1	
	Use of $F = \mu R$ to get an equation in μ only $[3.3g - 2.4g\mu \cos 30 - 2.4g \sin 30 = 0]$	DM1	Must be from F dimensionally correct and single term R which is equal to a component the 2.4 kg weight. Allow consistent sin/cos mix but must be different components of weight. F and R must be numerical expressions.
	$\mu = 1.01$ [sight of 1.01036... or 1.0104]	A1	AG perhaps from one of $\mu = \frac{3.3g - 2.4g \sin 30}{2.4g \cos 30} = \frac{3.3 - 1.2}{12\sqrt{3}} = \frac{2.1}{12\sqrt{3}} = \frac{7\sqrt{3}}{12} = \frac{21}{20.7846...}$ $= \frac{21}{20.8}$ Do not allow unless evidence of 30 substituted for θ . E.g.: sight of 1.01036... or 1.0104.
		5	

Question	Answer	Marks	Guidance
(b)	Using Newton's second law for both particles or the system	M1*	Must have correct number of terms. Allow sign errors. Allow sin/cos mix. Allow g missing. Masses must be appropriate for their equation(s). Forces must have components (or not) as required.
	Either $3.3g - T = 3.3a$ and $T - F - 2.4g \sin 20 = 2.4a$ $[T - 22.778 - 8.208 = 2.4a]$ or $[T - 30.986 = 2.4a]$ or $3.3g - F - 2.4g \sin 20 = (2.4 + 3.3)a \quad [2.013367... = 5.7a]$	A1	Both correct or system equation correct. Can be with a wrong non-zero F .
	$F = 1.01 \times 2.4g \cos 20 \quad [= 22.778]$	B1	For correct expression for F .
	Attempt to solve for $a \quad a = 0.353 \quad [0.353222...]$	DM1	Using their F Must get to ' $a =$ '. If sin/cos mix must be consistent.
	$v^2 = 2 \times 0.353 \times 1 \quad [= 0.706444...] \text{ or } [v = 0.841]$ Or $1 = 0 + \frac{1}{2} \times 0.353t^2 \Rightarrow t = 2.3795 \Rightarrow v = 0.353 \times 2.38$	A1FT	FT their value of $a \neq \pm g$ to get an expression for v^2 or v . Can be implied by awrt 0.84 for v or awrt 0.71 for v^2 . This mark does not depend on previous A or B mark, but both Ms must have been awarded.
	Using Newton's second law on A after B reaches the ground $-F - 2.4g \sin 20 = 2.4a$ $[-1.01 \times 2.4g \cos 20 - 2.4g \sin 20 = 2.4a]$ $[-22.78814... - 8.20848... = 2.4a]$	M1*	Must have correct number of terms. Allow sign errors. Allow sin/cos mix. Allow g missing. $[\Rightarrow a = -12.911...]$
	Use of suvat to find s $[0 = \text{their } 0.841^2 + 2 \times \text{their } -12.911... \times s \Rightarrow s = 0.027358...]$	DM1	Using their $a \neq \pm g$. Must get to ' $s =$ '. May find and use $t = 0.0651$.

Question	Answer	Marks	Guidance
(b)	Total distance = 1.03 m	A1	
		8	
	Alternative method using energy for first 5 marks		
	$[\text{KE gained}] = \frac{1}{2} \times (2.4 + 3.3)v^2 [= 2.85v^2]$	B1	
	$[\text{PE lost}] = 3.3g \times 1 - 2.4g \times 1 \sin 20 [= 24.791...] =$	B1	Allow omission of 1 in either or both terms.
	$[\text{Friction}] = 1.01 \times 2.4g \cos 20 [= 22.778...]$	B1	For correct expression for F .
	$\frac{1}{2} \times (2.4 + 3.3)v^2 = 3.3g \times 1 - 2.4g \times 1 \sin 20 - 1.01 \times 2.4g \cos 20 \times 1$ Or $2.85v^2 = 24.791... - 22.778...$	M1	For attempt at energy equation. Allow sign errors, allow sin/cos mix but must have sin/cos where needed. Correct number of terms, dimensionally correct. Allow omission of 1 in any or all the three relevant terms. Must have cos 20 and sin 20.
	To get a correct expression for v^2 $[v^2 = 0.706444... \text{ or } v = 0.841...]$	A1	Can be implied by awrt 0.84 for v or awrt 0.71 for v^2 if expression not seen.
Question	Answer	Marks	Guidance
(b)	Alternative method using energy for final 3 marks		
	$\text{KE} = \frac{1}{2} \times 2.4 \times 0.841^2$	M1	Using their v^2 .
	$1.01 \times 2.4g \cos 20 \times s + 2.4g \sin 20 \times s = \frac{1}{2} \times 2.4 \times 0.841^2$ $[\Rightarrow s = 0.027358...]$	M1	For attempt at 3 term energy equation and solved to get to ' $s =$ '. Allow sign errors, allow consistent sin/cos mix but must have sin/cos where needed. Correct number of terms, dimensionally correct.
	Total distance = 1.03 m	A1	

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12. 9709_m22_ms_42 Q: 5

Question	Answer	Marks	Guidance
(a)	Attempt to resolve vertically or horizontally	M1	Correct number of terms.
	$G \sin 60^\circ + 2F \sin 40^\circ - 10 = 0$	A1	Correct resolution vertically.
	$F + G \cos 60^\circ - 2F \cos 40^\circ = 0$	A1	Correct resolution horizontally.
	Attempt to solve simultaneously for F or G	M1	From equations with 3 relevant terms in each
	$F = 4.53, G = 4.82$	A1	For both correct.
		5	
(b)	$G \sin 60^\circ + 2 \times 3 \sin 40^\circ - 10 = 0$	M1	Resolve forces parallel to the 10 N force and equate this expression to zero, 3 terms.
	$G = 7.09$ to 3 sf	A1	
		2	

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13. 9709_s22_ms_41 Q: 3

Question	Answer	Marks	Guidance
	For attempt at resolving horizontally or vertically	M1	Allow sin/cos mix. Allow sign error. Allow g missing. Correct number of terms.
	$R = 300g - 0.28X$ or $R = 300g - X \sin 16.3$	A1	$\alpha = 16.26\dots$
	$0.96X - F = 0$ or $0.96X - 0.5(300g - X \sin \alpha) = 0$ Or $X \cos 16.3 - F = 0$ or $X \cos 16.3 - 0.5(300g - X \sin \alpha) = 0$	A1	Or using <i>their</i> F
	Use of $F = 0.5R$	M1	Use to get an equation in X only. Allow sin/cos mix. Allow sign error. Allow g missing. Must be from 2 term R , which is a linear combination of $300(g)$ and a component of X
	$X = 1360$ [1363.63...]	A1	
		5	

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14. 9709_s22_ms_41 Q: 4

Question	Answer	Marks	Guidance
	Attempt to resolve in any direction	M1	For resolving. Allow sin/cos mix. Allow sign error. Correct number of terms.
	$F \cos \alpha - 20 \cos 40 - 100 \sin 20 = 0$ [$F \cos \alpha = 15.320\dots + 34.202\dots = 49.5229\dots$]	A1	
	$F \sin \alpha + 20 \sin 40 - 100 \cos 20 = 0$ [$F \sin \alpha = 93.969\dots - 12.855\dots = 81.1135\dots$]	A1	
	$F = \sqrt{(49.5229\dots)^2 + (81.1135\dots)^2}$	M1	OE; Attempt to solve for F ; one term missing in total
	$\alpha = \tan^{-1} \left(\frac{81.1135\dots}{49.5229\dots} \right)$	M1	OE; Attempt to solve for α ; one term missing in total
	$F = 95(.0)$, $\alpha = 58.6$	A1	$F = 95.0364\dots$ and $\alpha = 58.5943\dots$
Alternative mark scheme for question 4: For candidates who use cosine and/or sine rule			
	Attempt at cosine rule from triangle of forces	M1	Must use lengths 100 and 20 with a suitable angle
	$F^2 = 100^2 + 20^2 - 2 \times 100 \times 20 \cos 70$	A1	Correct
	$F = 95[.0]$	A1	
	$\frac{95.0364}{\sin 70} = \frac{20}{\sin \beta}$ OR $\frac{95.0364}{\sin 70} = \frac{100}{\sin \gamma}$	M1	Attempt at sin rule
		A1	where $\beta = (70 - \alpha)$ where $\gamma = (40 + \alpha)$
	$\alpha = 58.6$	A1	$\alpha = 58.5943\dots$

Question	Answer	Marks	Guidance
	Alternative mark scheme for question 4: For candidates who resolve in other directions		
	Attempt to resolve (e.g. parallel or perpendicular to 100 N)	M1	For resolving. Allow sin/cos mix. Allow sign error. Correct number of terms.
	$F \sin(\alpha + 20) + 20 \sin 20 - 100 = 0$ [$F \sin(\alpha + 20) = 93.159\dots$]	A1	
	$F \cos(\alpha + 20) - 20 \cos 20 = 0$ [$F \cos(\alpha + 20) = 18.793\dots$]	A1	
	$F = \sqrt{93.159\dots^2 + 18.793^2}$	M1	OE; Attempt to solve for F ; one term missing in total
	$\alpha = \tan^{-1}\left(\frac{93.159\dots}{18.793\dots}\right) - 20$	M1	OE; Attempt to solve for α ; one term missing in total
	$F = 95[.0], \alpha = 58.6$	A1	$F = 95.0364\dots$ and $\alpha = 58.5943\dots$
		6	

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15. 9709_s22_ms_42 Q: 2

Question	Answer	Marks	Guidance
	Resolving either direction	M1	3 terms; allow sign errors and allow sin/cos mix
	$(X =) \pm (20 \cos 60 - 14 - 16 \cos 50)$ [$= \mp 14.2846\dots$]	A1	
	$(Y =) \pm (60 - 20 \sin 60 - 16 \sin 50)$ [$= \pm 30.42278\dots$]	A1	
	$R = \sqrt{(14.2846\dots)^2 + (30.42278\dots)^2}$	M1	Attempt to solve for R ; one missing term in total
	$\theta = \tan^{-1}\left(\frac{30.42278\dots}{14.2846\dots}\right)$ [$= \tan^{-1}(2.1297\dots)$] OR $\alpha = \tan^{-1}\left(\frac{14.2846\dots}{30.42278\dots}\right)$ [$= \tan^{-1}(0.4596\dots)$]	M1	Attempt to solve for θ or α ; one missing term in total
	$R = 33.6 \text{ N}$ Direction is 64.8° above the 14 N force or 25.2° above the negative x -axis or 25.2° left of the 60 N force or bearing 335° or 115° anticlockwise from the positive x -axis	A1	Both correct. OE; allow 64.9, 25.1 Giving an angle only is insufficient. Direction may be seen on a diagram, with minimum of arrow on resultant. Arrows on both components only is A0 as it doesn't show the direction of the resultant. However the direction is stated, it must be able to be drawn uniquely.
		6	

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16. 9709_s22_ms_42 Q: 5

Question	Answer	Marks	Guidance
	Attempt at resolving parallel to the plane	*M1	3 terms. Allow sign errors, sin/cos mix. Allow g missing, otherwise dimensionally correct.
	$65 \cos 36 = 12g \times \sin 24 + F$	A1	$F = 3.777707 \dots$
	Attempt at resolving perpendicular to the plane	*M1	3 terms. Allow sign errors, sin/cos mix. Allow g missing, otherwise dimensionally correct.
	$12g \times \cos 24 = R + 65 \sin 36$	A1	$R = 71.419 \dots$
	Use $F = \mu R$ $\left[\mu = \frac{65 \cos 36 - 12g \times \sin 24}{12g \times \cos 24 - 65 \sin 36} = \frac{52.586 - 48.808}{109.625 - 38.206} = \frac{3.777 \dots}{71.419 \dots} \right]$	DM1	To get an equation in μ only. Dependent on two previous M marks. Allow g missing
	$\mu = 0.0529$	A1	Allow AWRT 0.053 Do not accept fractional equivalent.
		6	

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17. 9709_s22_ms_43 Q: 4

Question	Answer	Marks	Guidance
(a)	$T_A \times 0.8 - T_B \times 0.6 - 20 = 0$ or $T_A \times 0.6 + T_B \times 0.8 - 10g = 0$	M1	Resolving horizontally or vertically
	$T_A \times 0.8 - T_B \times 0.6 - 20 = 0$	A1	
	$T_A \times 0.6 + T_B \times 0.8 - 10g = 0$	A1	
	$0.8T_A - \frac{0.6(10g - 0.6T_A)}{0.8} = 20 \rightarrow T_A = \dots$	M1	Attempt to solve simultaneously
	$T_A = 76 \text{ N}, T_B = 68 \text{ N}$	A1	
		5	

Question	Answer	Marks	Guidance
(b)	$T_A \times 0.6 - 10g = 0 \Rightarrow T_A = \frac{500}{3}$	B1	From using $T_B = 0$
	$T_A \times 0.8 - F = 0$	M1	
	$F = \frac{400}{3}$	A1	Allow $F = 133$ to 3 s.f.
		3	

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